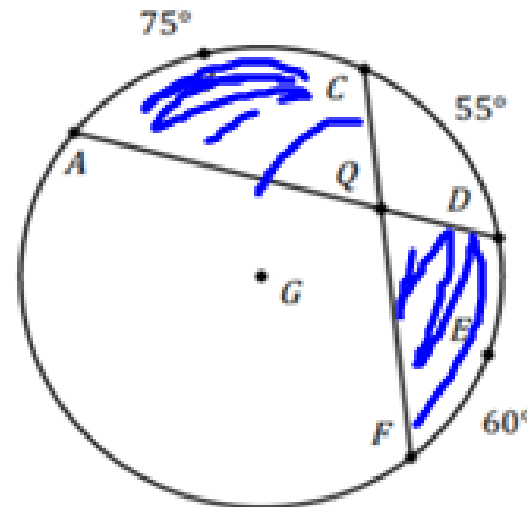
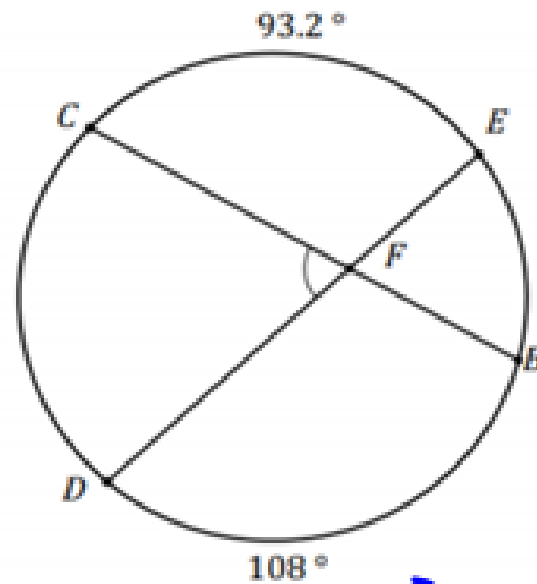


1. Consider the figure below, and determine $m\angle AQC$.



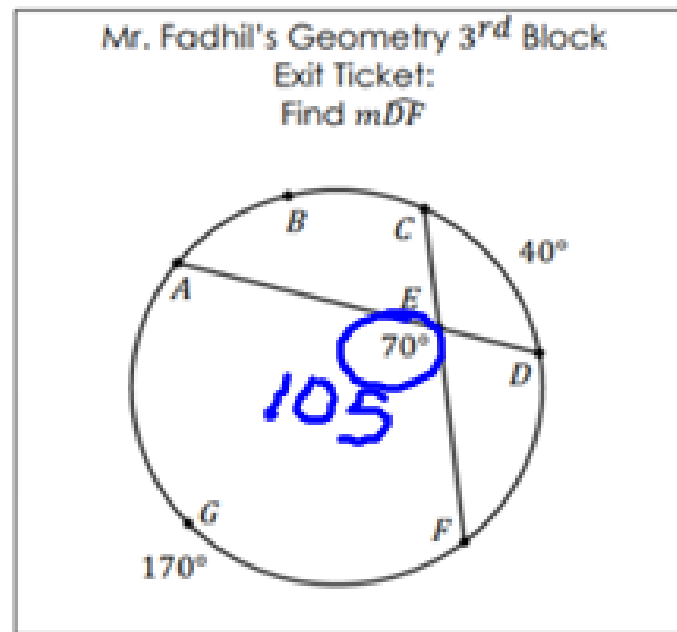
$$\frac{1}{2} (75 + 60) = m\angle AQC$$
$$\frac{1}{2} (135) = 67.5^\circ$$

2. Consider the diagram below and find $m\angle CFD$. Justify your answer.



$$\begin{aligned}\frac{1}{2} (108 + 93.2) &= m\angle CFE \\ &= 100.6 \\ 180 - 100.6 &= m\angle CFD \\ &= 79.4\end{aligned}$$

Mr. Fadhil gave the daily exit ticket shown in the diagram to his Geometry students.



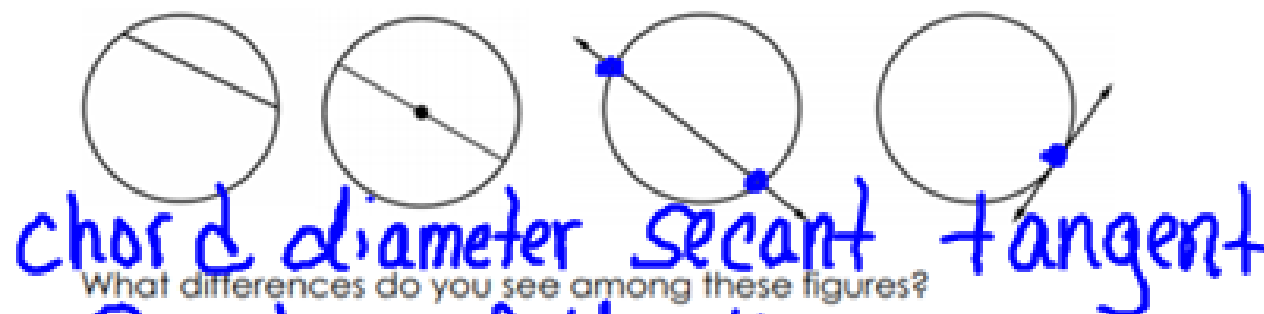
One of Mr. Fadhil's students argued that there was something wrong with this problem, based on the above diagram and the measurements.

What is the error in this problem? Justify your answer.

$$\frac{1}{2}(170 + 40) = 105 \neq 70$$

Tangent Lines, Secants, and Chords – Part 1

Let's examine the following figures.



Position of the lines
Segments & lines

Which of these figure(s) have you not seen yet?

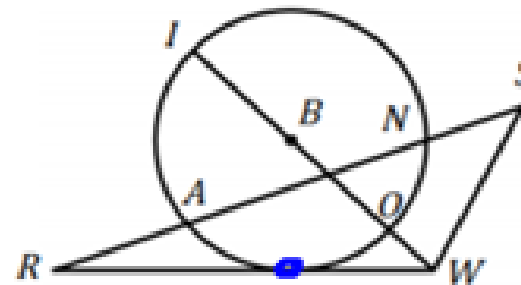
The last 2

A **secant** is a line that intersects a circle at 2 points.

A **tangent** is a line in the plane of a circle that intersects the circle at exactly 1 point.

1. Classify each of the following segments as a radius, chord, secant, tangent, or diameter.

\overline{TB} is a radius
 \overline{AN} is a chord
 \overline{WR} is a tangent
 \overline{RS} is a secant
 \overline{IO} is a diameter



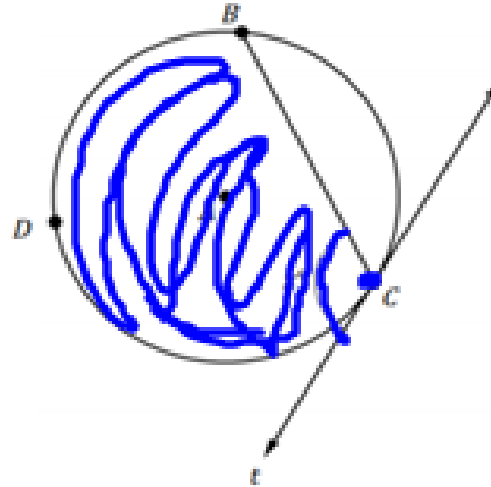
2. Mark the most appropriate answer for each statement in the table below.

Statements	Always	Sometimes	Never
A chord is part of a secant.	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
A diameter is a tangent.	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
A tangent is a ray.	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
A tangent has exactly one point in common with a circle.	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
A secant to a circle contains the diameter.	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
A chord in a circle contains a radius.	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>

Consider the diagram below.



$$x = \frac{1}{2} m \widehat{AC}$$



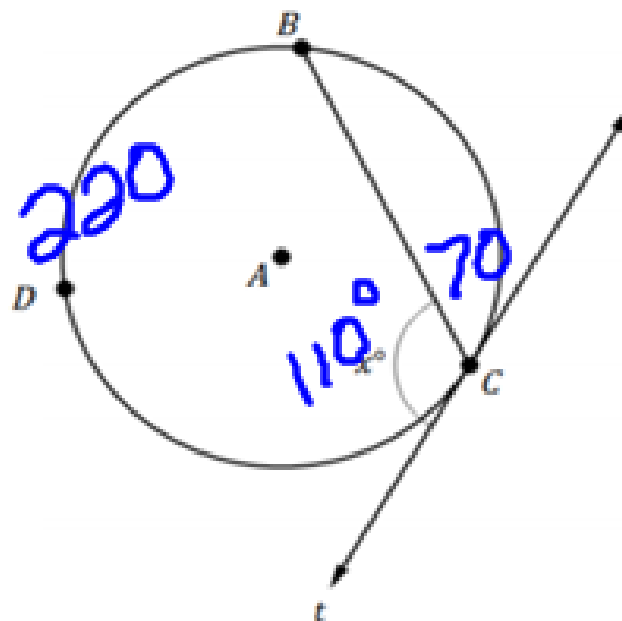
Circle A has chord \overline{BC} and tangent line t through C . The chord and the tangent line form an angle measuring x° . What do you think is the value of x in the above figure?

$$x = \frac{1}{2} m \widehat{BDC}$$

Tangent-Chord Angle Theorem

The measure of an angle formed by a chord and a tangent line is $\frac{1}{2}$ the measure of the intercepted arc.

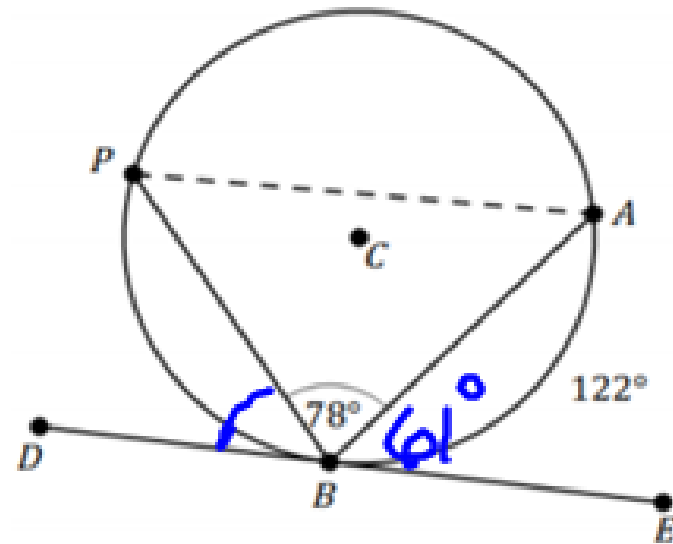
1. Consider the diagram below.



If $m\widehat{CDB}$ is 220° , then what is the supplement of the angle measuring x° ? Justify your answer.

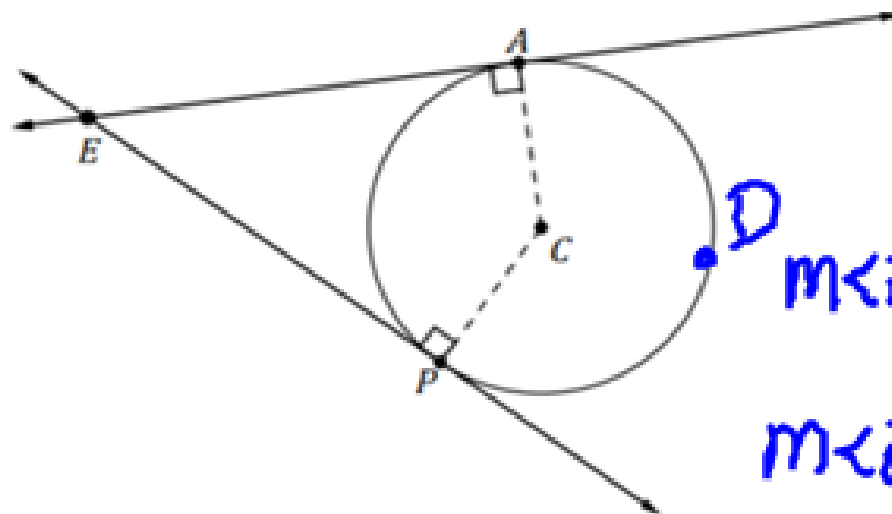
$$\frac{220}{2} = 110^\circ$$
$$= 180$$
$$- 110$$
$$= 70^\circ$$

Consider the diagram below.



a. Determine the $m\angle PBD$.

$$\frac{122}{2} = 61^\circ$$
$$\begin{array}{r} 78 \\ + 61 \\ \hline 139 \end{array}$$
$$\begin{array}{r} 180 \\ - 139 \\ \hline 41^\circ \end{array}$$



$$m\angle E = \frac{1}{2} (m\widehat{ADP} - m\widehat{AP})$$

$$m\angle E + m\angle C = 180^\circ$$

$\angle AEP$ is a Circumscribed angle.

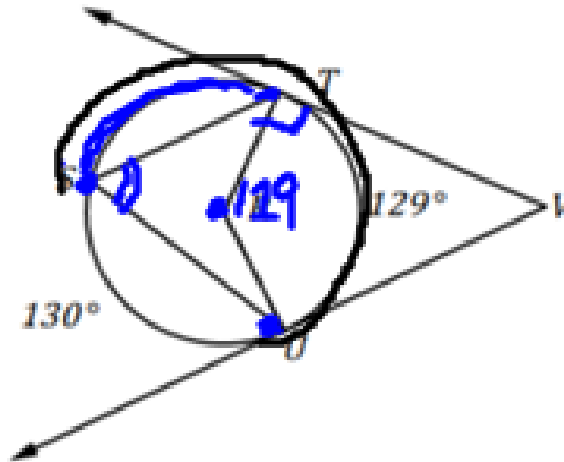
A Circumscribed angle is an angle with rays tangent to the circle. It is equal to $\frac{1}{2}$ of the difference between the intercepted arcs.

The Circumscribed angle and the Central angle formed by the same arcs are supplementary angles.

Let's Practice!

3. Find each of the following angles and arcs formed in circle R .

- a. $m\angle RTV = 90$
 b. $m\angle TRU = 129$
 c. $m\angle TVU = 51$
 d. $m\angle TSU = 64.5$
 e. $m\widehat{ST} = 101$
 f. $m\widehat{STU} = 230$



$$\begin{array}{r} 180 \\ - 129 \\ \hline 51 \end{array}$$

$$\frac{129}{2} = 64.5$$

$$\begin{array}{r} + 129 \\ + 130 \\ \hline 259 \end{array} \quad \begin{array}{r} 360 \\ - 259 \\ \hline 101 \\ + 129 \\ \hline 230 \end{array}$$