

An arc has a length of  $4\pi$  units and a radius of 6 units. What is the angle of the sector in radians?

$$\frac{1 \cancel{4\pi}}{3 \cancel{12\pi}} = \frac{x}{360}$$

$$\frac{1}{3} = \frac{x}{360}$$

$$360 = 3x \quad x = 120$$

$$\frac{2 \cancel{120\pi}}{\cancel{180}} = \frac{2\pi}{3}$$

Suppose a circle with an 11.4 inch arc intercepted by the central angle and a radius that is 3 inches long. Determine the measure of the central angle in radians.

$$\frac{11.4}{6\pi} = \frac{x}{360}$$

$$\frac{4,104}{18.8496} = \frac{18.8496x}{18.8496}$$

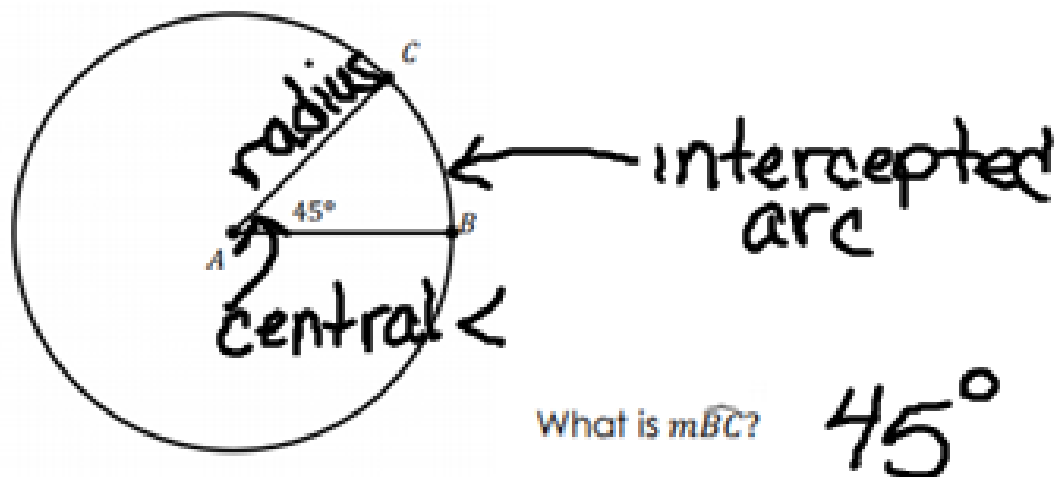
$$217.7235 = x$$

217.7235

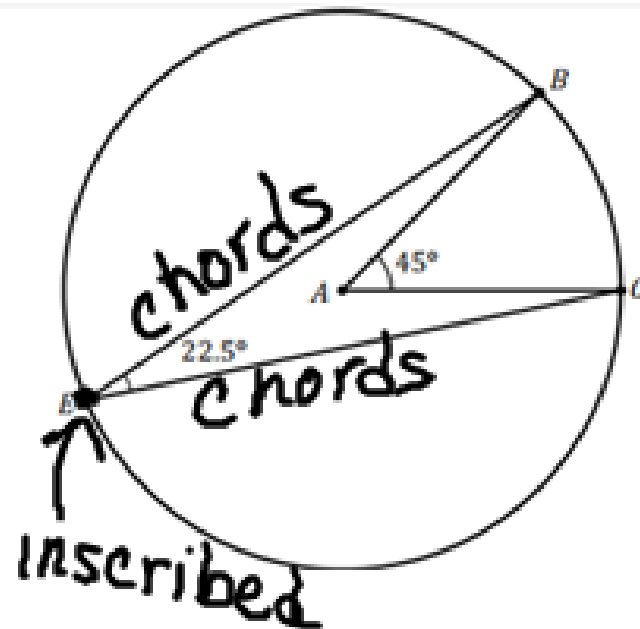
$$\frac{1.2\pi}{180}$$

$$\frac{\pi}{180}$$

The measure of an arc on a circle is equal to the degree measure of the central  $\angle$  that intercepts the arc.



Consider the figure below.  $\angle E$  is an inscribed angle.  $\widehat{BC}$  is an intercepted arc by both the central angle  $\angle A$  and the inscribed angle.



Define the inscribed angle.

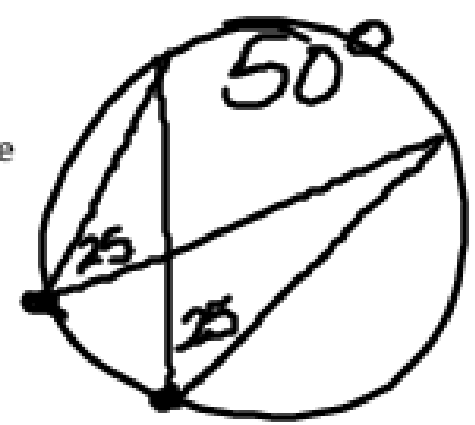
$$\text{inscribed } \angle = \frac{1}{2} \text{central } \angle$$

Compare and contrast the inscribed angle and the intercepted arc.

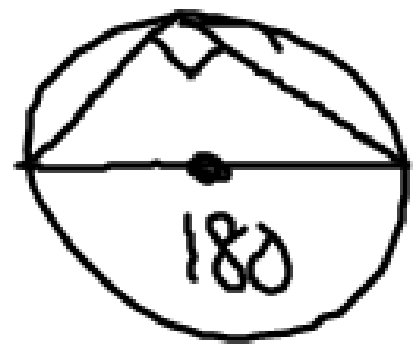
$\text{inscribed} = \frac{1}{2} \text{ intercepted arc}$   
Inscribed Angle Conjectures

In a circle, the measure of an inscribed angle is  $\frac{1}{2}$  the measure of the central angle with the same intercepted arc.

In a circle, two inscribed angles with the same intercepted arc are congruent.

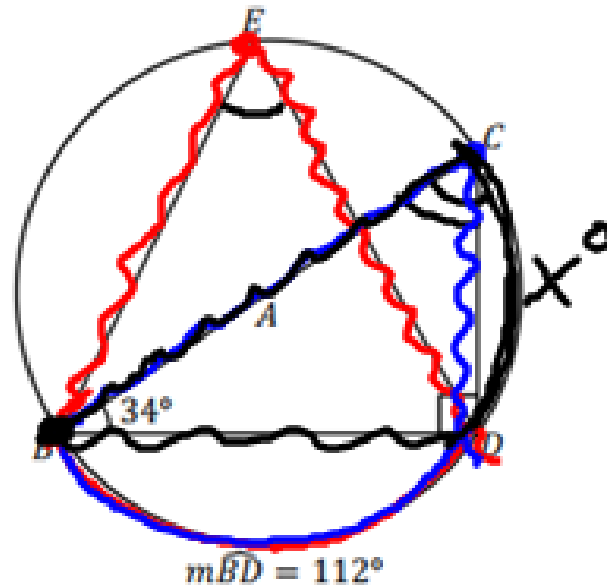


Any angle inscribed in a semicircle is a Right angle.



**Practice:**

Consider circle A in the following figure, and find  $m\angle BED$ ,  $m\angle BCD$ , &  $m\widehat{CD}$ .



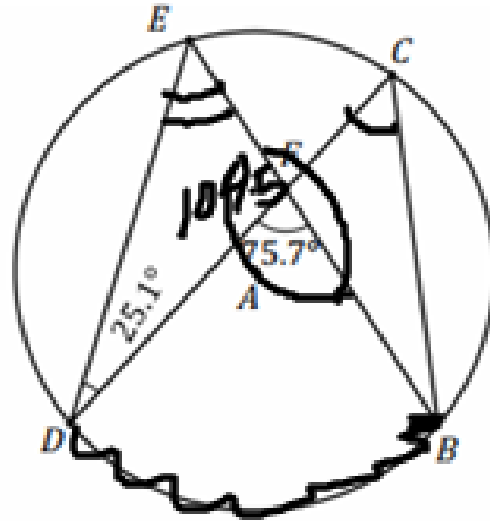
$$m\angle BED = \frac{112}{2} = 56^\circ$$

$$m\angle BCD = 56^\circ$$

$$34(2) = 68^\circ \\ = m\widehat{CD}$$

Your turn:

Consider circle A in the following figure, and find  $m\angle BCF$ ,  $m\angle BED$ , &  $m\widehat{DB}$ .



$$\begin{array}{r} 180 \\ - 75.7 \\ \hline \end{array}$$

$$\begin{array}{r} 104.3 \\ + 25.1 \\ \hline \end{array}$$

$$\begin{array}{r} 129.4 \\ \hline \end{array}$$

$$\begin{array}{r} 180 \\ - 129.4 \\ \hline \end{array}$$

$$50.6$$

$$\angle BCF = 50.6$$

$$\angle BED = 50.6$$

$$50.6(2)$$

$$101.2 = \widehat{DB}$$